University of Waterloo STAT 221 – J. C. Robinson

Assignment 3

A3-1. Listed below are the defects identified by 100% inspection of the first 19,986 plastic trim items produced at *XYZ Automotive*; a legend for the six defect codes is given at the right below the lists. The first day's production was 12,439 items and the second day's was 7,547 – there was a breakdown in the process at 11.34 a.m. on the second day.

January 5:		A B C D B C A E A C C C E C C C E C E C E C E C A D B C E B A D B D C B C C A B C
		(OPERATOR TEMPORARILY REPLACED)
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January 6:		C F C E E E B E E E E E D A B E C E E C E E C E E E B F E B E E B E A E F E E E E B E E E E C C A B E C C

- (a) Carry out a Pareto analysis on each day's production.
- (b) Compare the two Pareto diagrams; comment briefly on important similarities and differences.
- (c) A replacement operator was called in at short notice just before noon on January 5, but on January 6 the regular operator returned; examine the January 5 data for evidence of an operator effect. Briefly explain your findings.
- A unfill on outer surface
- B unfill on inner surface
- C visual defect on outer surface
- D colour out of specification
- E surface scratch
- F other
- A3 2. Coffee doesn't taste the way it used to. said one member of the coffee club. The coffee is strong enough but it doesn't have the taste I like any more. Using **brainstorming** (preferably with a group of up to four other members of the class), make a cause-and-effect diagram to properly display factors that might be responsible for these comments. Assume a domestic electric coffee maker is used, and add any relevant additional comments below you diagram.

NOTE: Clearly indicate either the names of the members of your group or that you worked alone.

- A3 3. A sample of 200 braces is obtained by equiprobable selecting from a supplier's latest shipment and each brace is measured; the data are tabulated below. The print calls for 92-108 cm.
 - (a) Suggest how equiprobable selecting might be implemented in practice in a situation like this.
 - (b) Construct an appropriate histogram of the data.
 - (c) On the basis of your histogram, comment briefly on the supplier's manufacturing process.

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99.6 98.2 106.0 101.4
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                                                                      93.6 103.9 106.4 104.7 103.0
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- A3-4. The diameter of a production lot of rotor shafts has an average of 0.239 cm and a standard deviation of 0.003 cm. Calculate a specification such that 99.7% of production will fall within the specification limits. State clearly any assumption(s) underlying your calculations.
- A3-5. Monitoring over time of the amount of swell of plastic rods coming from an extruder has found it is stable with an average of 13.9% and a standard deviation of 0.55%; histograms have shown that the pattern of variation of the percentage swell can be modelled by a normal distribution. The specification limits for the swell are 12.0-15.0%.
 - (a) Find the proportion of the production that is out of specification. In a production run of 10,000 rods, how many would be expected to be out of specification?
 - (b) Suppose that the average percentage swell could be altered from 13.9% to 13.5% by adjusting the process, what proportion of the production would be out of specification? State clearly any assumption(s) involved in your calculation. Give a simple graphical portrayal of the situation before and after adjustment.
 - (c) Suppose that the *next* swell reading after the process has supposedly been adjusted as in (b) is 15.4%. What Answer can reasonably be given to the Question about the value of the process average? Show your reasoning clearly.