

AMATH 250

Final Exam Information

Date: Thursday, April 20

Time: 12:30–3:00 p.m.

Place: PAC, Area 4

Office hours (MC 5124):

Tuesday April 18, Wednesday April 19, 1-4 p.m.

Or by appointment: sacampbell@uwaterloo.ca, 888-4567 ext. 5461

Material Covered:

All material covered in lectures and assignments.

All material covered in the Course Notes except sections 1.2.5 and 1.2.6.

Approximately 60% of exam will be on material since the midterm.

Statements of all theorems and definitions given in the Course Notes.

The proofs of the following theorems:

Chapter 3: Superposition Principle for Homogeneous DEs (Proposition, p. 53)

Chapter 4: First Shift Theorem (p. 85)

Derivative Theorem (Proposition 1, p. 85)

Chapter 5: Laplace Transform of $\mathbf{Ax}$ (Proposition 2, p. 112)

Derivative property for fundamental matrices (Proposition 1, p. 124)

Practice Problems:

Course Notes: Problem Sets

Reserve books:

Borrelli and Coleman (QA 371.B74 2004)

Sections 1.1-1.3, 2.1-2.2, 2.5, 3.1-3.7, 4.1-4.4, 5.1-5.2, 6.1-6.5

Boyce and DiPrima (QA 372.B73 1992)

Sections 2.1-2.7, 3.1-3.2, 3.4-3.6, 3.8-3.9, 6.1-6.4, 7.1, 7.5-7.9

Edwards and Penny (QA 371.E28 2004)

Sections 1.1, 1.2, 1.4, 1.5, 3.3-3.7, 5.1-5.4, 5.6, 7.1-7.4

You will be given the formula sheet on the reverse with your exam.

Final Grade: will be calculated as the greater of

(10% Assignments (best 9 of 10) + 25% midterm + 65% final) or (100% final)

AMATH 250 Formula Sheet

Laplace Transforms

$f(t) = \mathcal{L}^{-1}\{F(s)\}$	$F(s) = \mathcal{L}\{f(t)\}$
e^{at}	$\frac{1}{s-a}$
$\cos(bt)$	$\frac{s}{s^2+b^2}$
$\sin(bt)$	$\frac{b}{s^2+b^2}$
t^n	$\frac{n!}{s^{n+1}}$
$e^{ct}f(t)$	$F(s-c)$
$H(t-c)f(t-c)$	$e^{-cs}F(s)$
$f'(t)$	$sF(s) - f(0)$
$(-t)^n f(t)$	$F^{(n)}(s)$

Partial Fractions

$$\begin{aligned}\frac{1}{(s+a)(s+b)} &= \frac{1}{a-b} \left(\frac{1}{s+b} - \frac{1}{s+a} \right) \\ \frac{s}{(s+a)(s+b)} &= \frac{1}{a-b} \left(\frac{a}{s+a} - \frac{b}{s+b} \right) \\ \frac{1}{(s+a)(s^2+b^2)} &= \frac{1}{a^2+b^2} \left(\frac{1}{s+a} + \frac{a-s}{s^2+b^2} \right) \\ \frac{s}{(s+a)(s^2+b^2)} &= \frac{1}{a^2+b^2} \left(-\frac{a}{s+a} + \frac{b^2+as}{s^2+b^2} \right) \\ \frac{1}{(s^2+a^2)(s^2+b^2)} &= \frac{1}{b^2-a^2} \left(\frac{1}{s^2+a^2} - \frac{1}{s^2+b^2} \right) \\ \frac{s}{(s^2+a^2)(s^2+b^2)} &= \frac{1}{b^2-a^2} \left(\frac{s}{s^2+a^2} - \frac{s}{s^2+b^2} \right)\end{aligned}$$

Trigonometric Identities

$$\begin{aligned}\cos(A+B) &= \cos A \cos B - \sin A \sin B \\ \sin(A+B) &= \sin A \cos B + \cos A \sin B \\ \cos A - \cos B &= -2 \sin \left(\frac{A+B}{2} \right) \sin \left(\frac{A-B}{2} \right)\end{aligned}$$