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RnavGraph

Interactive visual clustering

**Adrian Waddell
and Wayne Oldford**

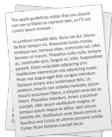
SSC June 14, 2011

Challenge

- ▶ p values on each of n individuals

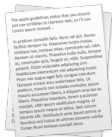
Challenge

- ▶ p values on each of n individuals
- ▶ data can have a complex structure



Challenge

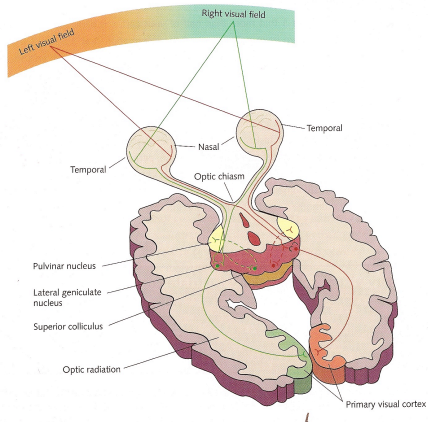
- ▶ p values on each of n individuals
- ▶ data can have a complex structure



- ▶ n , or p , or both can be very large

Why Visualization?

- ▶ powerful human visual system
 - ▶ patterns, relations, textures,...
 - ▶ recognize structure
 - ▶ discover structure
- ▶ data analysis objectives
 - ▶ relations, clusters, classes, outliers, diagnostics, unusual structure, ...



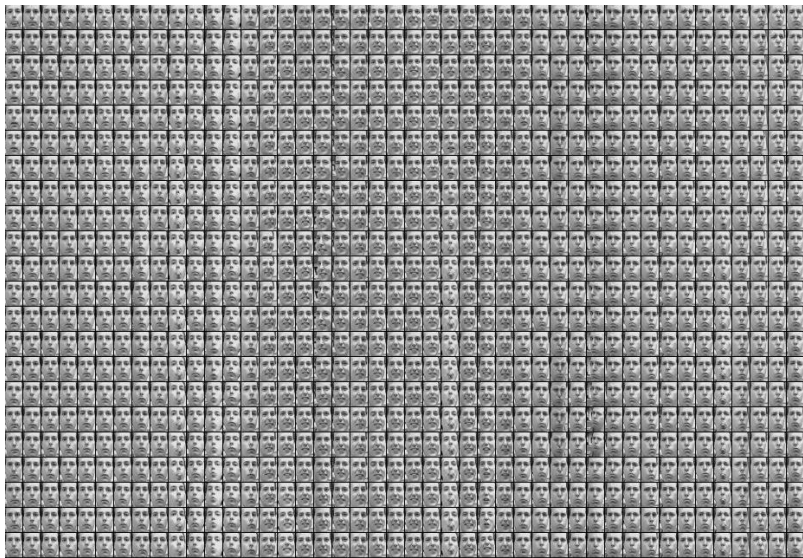
Dealing with high dimensionality \rightarrow large p

- ▶ visually, we are constrained to small p
 - ▶ locations: $p < 4$
 - ▶ use color, shape, texture, movement,...
- ▶ large number of low dimensional views
 - ▶ $\binom{p}{d}$ d -dimensional views
 - ▶ How? Which ones? And, in what order?

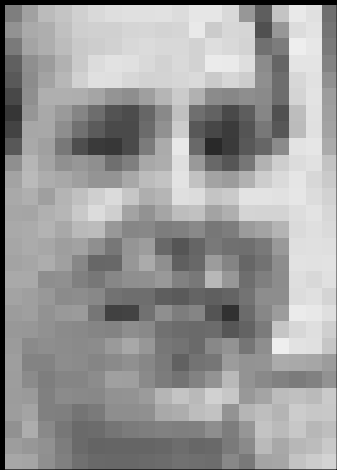
Proposed Approach

- ▶ reduce numbers
 - ▶ p overall dimensionality
 - ▶ $\binom{p}{d}$ subset of all low-d views
- ▶ interactive/tailored low-d views
- ▶ connect low-d views via interactive navigation graphs

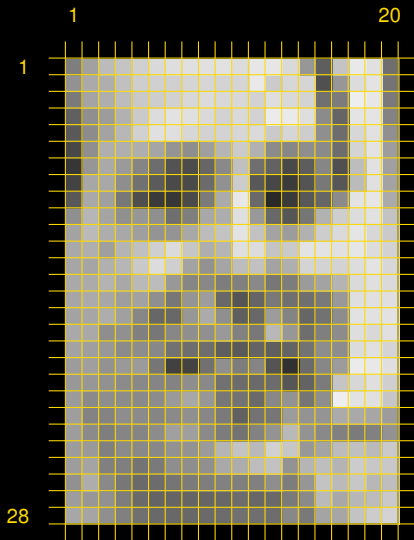
Example: Frey faces from 1965 movie frames



Reduce dimensionality

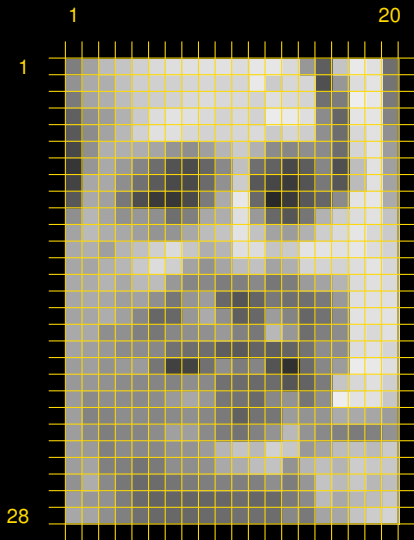


Reduce dimensionality



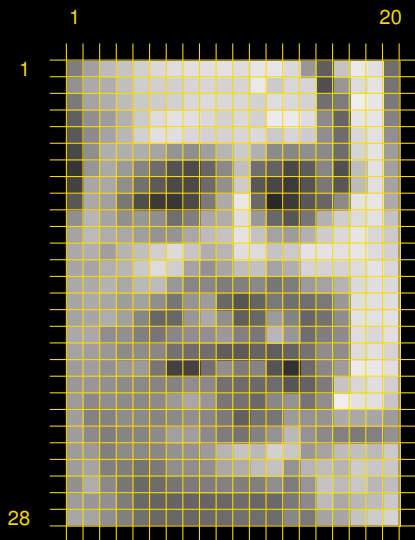
▶ $28 \cdot 20 = 560$ dimensions

Reduce dimensionality



- ▶ $28 \cdot 20 = 560$ dimensions
- ▶ explore via low dimensional spaces

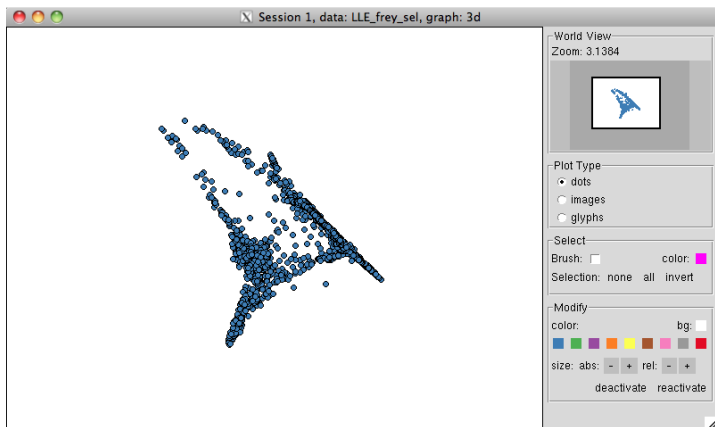
Reduce dimensionality



- ▶ $28 \cdot 20 = 560$ dimensions
- ▶ explore via low dimensional spaces
- ▶ Using **LLE**: local linear embedding
- ▶ $k = 12$ neighbors
- ▶ reduce to 5 dimensions

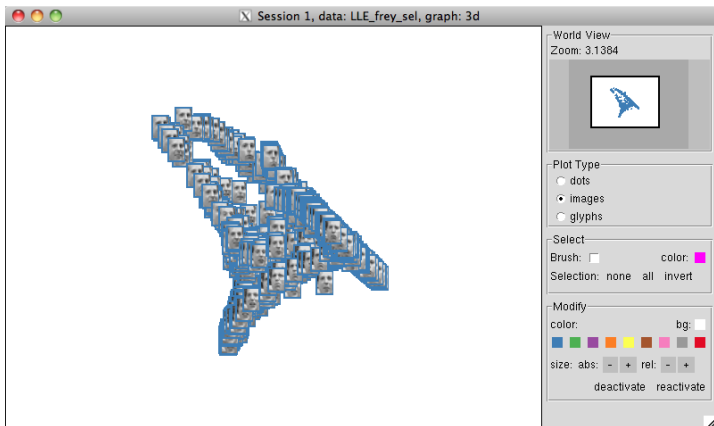
$$(x_1, x_2, x_3, x_4, x_5)$$

Interactive $2d$ view



► (x_1, x_2) - $2d$ dot plot

Interactive $2d$ view



► (x_1, x_2) - $2d$ image plot

Interactive *2d* view

- ▶ Point selection, brushing

- ▶ Deactivate complementary points

Interactive *2d* view

- ▶ Images, zoom, relocate

Interactive *2d* view

- ▶ Resize, zoom

Interactive *2d* view

- ▶ Zoom out, reactivate, resize, pan

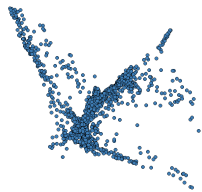
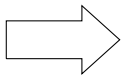
Interactive $2d$ view

- ▶ Zoom out, back to dots

Connecting the views



(x_1, x_2)

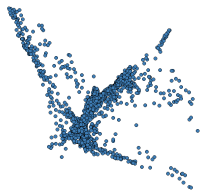
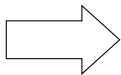


(x_2, x_3)

Connecting the views



(x_1, x_2)



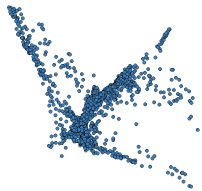
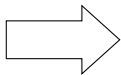
(x_2, x_3)

- ▶ 3d rigid rotation

Connecting the views

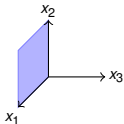


(x_1, x_2)



(x_2, x_3)

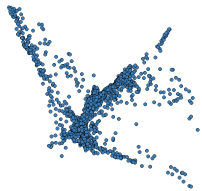
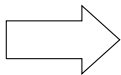
► 3d rigid rotation



Connecting the views

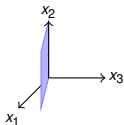
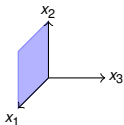


(x_1, x_2)



(x_2, x_3)

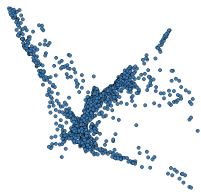
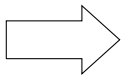
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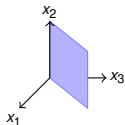
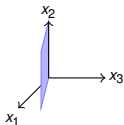
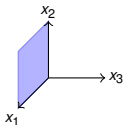


(x_1, x_2)

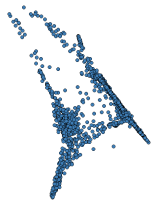


(x_2, x_3)

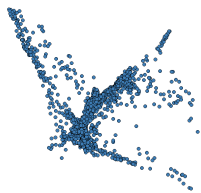
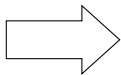
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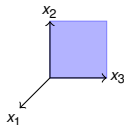
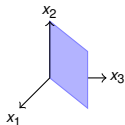
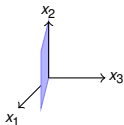
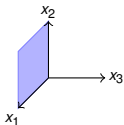


(x_1, x_2)



(x_2, x_3)

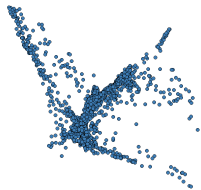
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Connecting the views



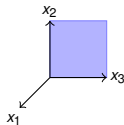
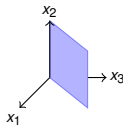
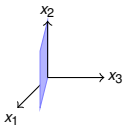
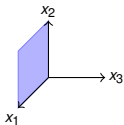
(x_1, x_2)



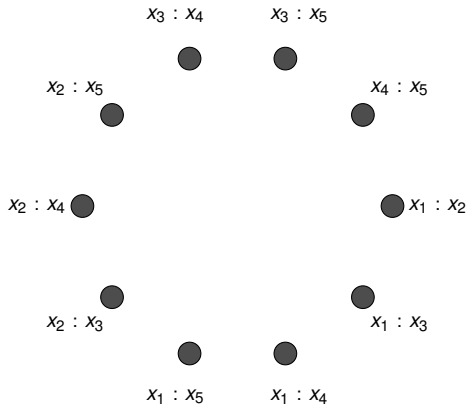
(x_2, x_3)

3d - transition

► *3d* rigid rotation



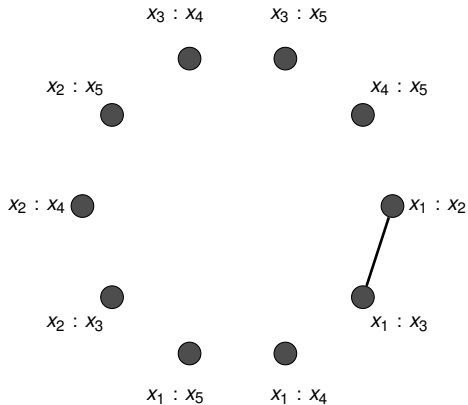
A 3d transition graph



► Each node is a 2d view

$$\binom{5}{2} = 10$$

A 3d transition graph

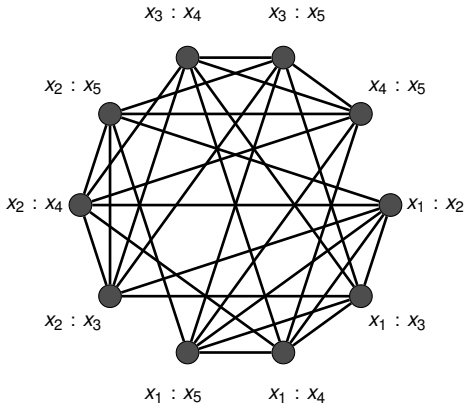


- ▶ Each node is a $2d$ view

$$\binom{5}{2} = 10$$

- ▶ Each edge is a $3d$ transition

A 3d transition graph

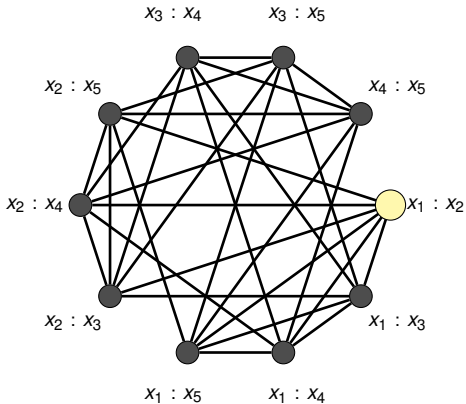


- ▶ Each node is a 2d view

$$\binom{5}{2} = 10$$

- ▶ Each edge is a 3d transition

A 3d transition graph



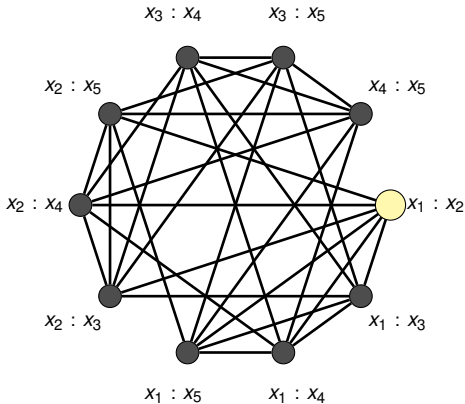
- ▶ Each node is a 2d view

$$\binom{5}{2} = 10$$

- ▶ Each edge is a 3d transition

- ▶  You are here bullet

A 3d transition graph



- ▶ Each node is a 2d view

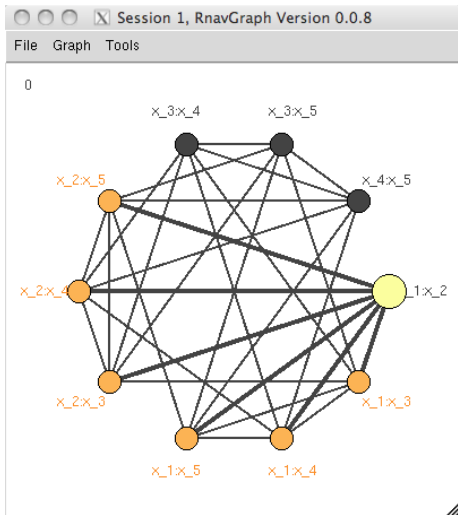
$$\binom{5}{2} = 10$$

- ▶ Each edge is a 3d transition

- ▶ ● You are here bullet

- ▶ This is a navigation graph (NavGraph)

A 3d transition graph



- ▶ Each node is a $2d$ view

$$\binom{5}{2} = 10$$

- ▶ Each edge is a $3d$ transition

- ▶  You are here bullet

- ▶ This is a navigation graph (NavGraph)

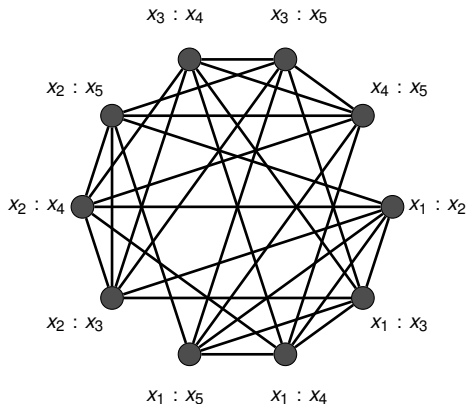
Interactive navigation graph

Move the bullet

2d view changes in response

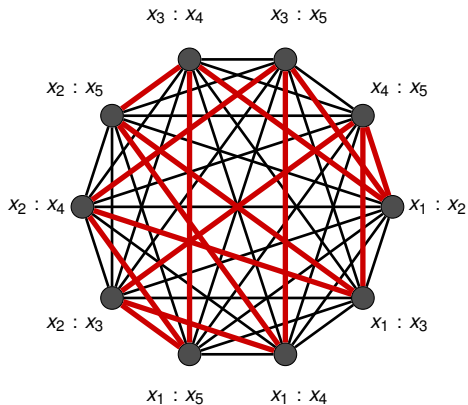
- ▶ Can stop anywhere and interact with the low-d view

3d and 4d transition graphs



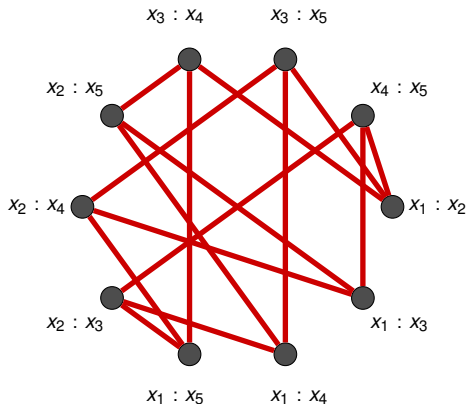
- complement of 3d transition graph yields 4d transition graph

3d and 4d transition graphs



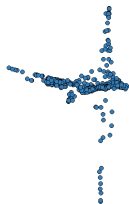
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3d and 4d transition graphs

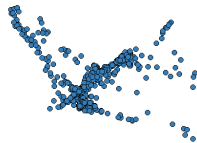


- complement of 3d transition graph yields 4d transition graph

4d transition $(x_1 : x_5) \rightarrow (x_2 : x_3)$

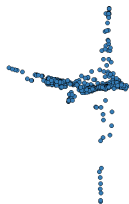


(x_1, x_5)

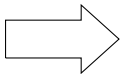


(x_2, x_3)

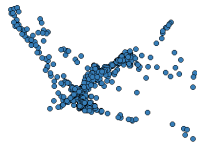
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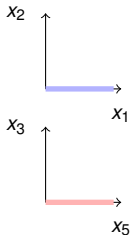
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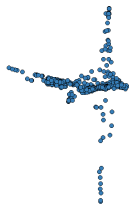
■ x-axis
■ y-axis



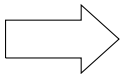
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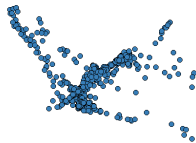
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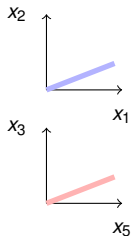
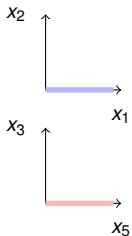
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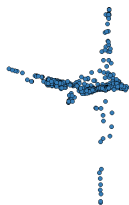
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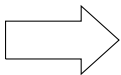
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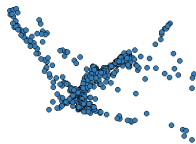
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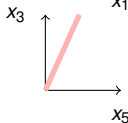
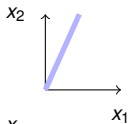
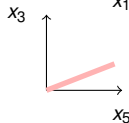
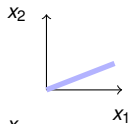
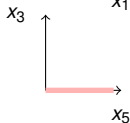
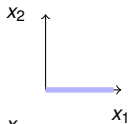
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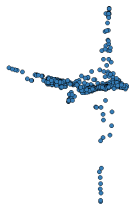
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y-axis



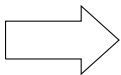
(x_2, x_3)



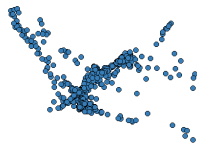
4d transition $(x_1 : x_5) \rightarrow (x_2 : x_3)$



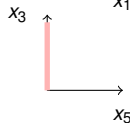
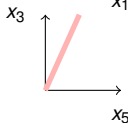
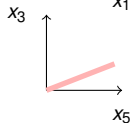
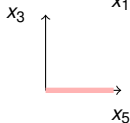
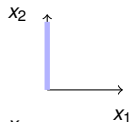
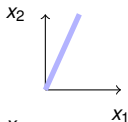
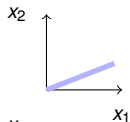
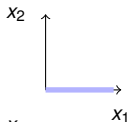
(x_1, x_5)



■ x-axis
■ y-axis



(x_2, x_3)



4d transition $(x_1 : x_5) \rightarrow (x_2 : x_3)$

- ▶ **4d transition is NOT a right rotation**

Try the package yourself

- ▶ This is only a part of our R package
- ▶ Try it yourself
- ▶ Package is on CRAN: `install.packages('RnavGraph')`
- ▶ Install dependencies and suggested packages
- ▶ Read the vignette
- ▶ Try the demos

▶ Oldford and Waddell

- ▶ Visual clustering of high-dimensional data by navigating low-dimensional spaces (**ISI Dublin, 2011**)
- ▶ RnavGraph: A visualization tool for navigating through high dimensional data (**ISI Dublin, 2011**)
- ▶ RnavGraph R package, available on CRAN

▶ Hurley and Oldford

- ▶ Graphs as a navigational infrastructure for high dimensional data spaces (**Comp Stats 2011**)
- ▶ Pairwise display of high dimensional information via Eulerian tours and Hamiltonian decompositions (**JCGS, 2010**)
 - ▶ Eulerian tour algorithms for data visualization and the PairViz R package (**Comp Stats 2011**)
 - ▶ **PairViz** R package, available on CRAN