# Rahim Nazim Moosa

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# Education

**Ph.D. in Mathematics** University of Illinois at Urbana-Champaign, 2001 Thesis: Contributions to the Model Theory of Fields and Compact Complex Spaces Advisor: Anand Pillay

B.ArtsSc. (Hons.)

McMaster University, 1996

# Academic Positions

**Professor** University of Waterloo July 2015 - present July-December 2021 Visiting Researcher Fields Institute, Toronto CARMIN Visiting Researcher IHES and IHP, Paris January-July 2018 Associate Professor University of Waterloo July 2009 - June 2015 Member MSRI, Berkeley January-May 2014 Scientific Member Max Planck Institute, Bonn, Germany April-June 2012 Assistant Professor University of Waterloo July 2004 - June 2009 Programme Participant Isaac Newton Inst., Cambridge, UK May-July 2005 CLE Moore Instructor MIT July 2002 - June 2004 NSERC Postdoctoral Fellow Fields Institute July 2001 - June 2002 Visiting Assistant Professor UC Berkeley August 2001 - May 2002

# **Individual Grants Awarded**

#### **NSERC Discovery Grants**

2005- present

Current: \$135,000 (2021–2026)

Past: \$100,000 (2015–2021), \$120,000 (2010–2015), \$80,000 (2005–2010)

NSERC Discovery Accelerator Supplement \$120,000

2015-2018

# **Editorial Positions**

Founding Editor-in-Chief Model Theory

Associate Editor

Canadian Journal of Math and Canadian Math Bulletin

2021 –

Reviews Editor The Bulletin of Symbolic Logic

2011 –

### Research Interests

Model theory (a branch of mathematical logic). Especially interactions with algebra and geometry.

# **Articles Under Review**

- 38. Bounding nonminimality and a conjecture of Borovik-Cherlin (with J. Freitag), Submitted, 22 pages.
- 37. Effective isotrivial Mordell-Lang in positive characteristic (with J. Bell and D. Ghioca), Submitted, 42 pages.

#### Refereed Publications

- 36. Model theory and the DME: a survey. To appear in Research Trends in Contemporary Logic (Eds M. Fitting et al), 17 pages.
- 35. Invariant hypersurfaces (with J. Bell and A. Topaz)
  To appear in the Journal de l'Institut de Mathématiques de Jussieu, 25 pages.
- 34. Internality of logarithmic-differential pullbacks (with R. Jin) Transactions of the American Mathematical Society, 373 (7):4863–4887, 2020.
- 33. F-sets and finite automata (with J. Bell) Journal de Théorie des Nombres de Bordeaux, 31 (1):101–130, 2019.
- 32. Isolated types of finite rank: an abstract Dixmier-Moeglin equivalence (with O. León Sánchez) Selecta Mathematica, 25 (2019), number 1, Art.10, 10pp.

31. Functoriality and uniformity in Hrushovski's groupoid-cover correspondence (with L. Haykazyan)

Annals of Pure and Applied Logic, 169 (8):715–730, 2018.

- 30. D-groups and the Dixmier-Moeglin equivalence (with J. Bell and O. León Sánchez) Algebra & Number Theory, 12 (2):343–378, 2018.
- 29. Finiteness theorems on hypersurfaces in partial differential-algebraic geometry (with J. Freitag)

Advances in Mathematics, 314:726–755, 2017.

28. Model theory of compact complex manifolds with an automorphism (with M. Bays and M. Hils)

Transactions of the American Mathematical Society, 369(6):4485–4516, 2017.

- 27. Poisson algebras via model theory and diffferential-algebraic geometry (with J. Bell, S. Launois, and O. Leon Sanchez)
  Journal of the European Mathematical Society, 19(7):2019–2049, 2017.
- 26. The model companion of differential fields with free operators (with O. Leon Sanchez)
  Journal of Symbolic Logic, 81(2):493–509, 2016.
- 25. Differential-algebraic jet spaces preserve internality to the constants (with Z. Chatzidakis and M. Harrison-Trainor)
  Journal of Symbolic Logic, 80(3):1022–1034, 2015.
- 24. A note on subvarieties of powers of OT-manifolds (with M. Toma) Bulletin de la Société des Sciences Mathématiques de Roumanie, 58(3):311–316, 2015.
- 23. Model theory of fields with free operators in characteristic zero (with T. Scanlon)

Journal of Mathematical Logic, 2014, doi: 10.1142/s0219061314500093. 38 pages

- 22. Some model theory of fibrations and algebraic reductions (with A. Pillay) Selecta Mathematica, 20(4):1067–1082, 2014
- 21. Countably categorical strongly minimal compact complex manifolds (with A. Pillay)

Proceedings of the American Mathematical Society, 140(5):1785–1801, 2012

20. Nonstandard methods for bounds in differential polynomial rings (with M. Harrison-Trainor and J. Klys) Journal of Algebra, 360:71–86, 2012

19. A model-theoretic counterpart to Moishezon morphisms
In Models, Logics and Higher-Dimensional Categories: A Tribute to the Work of Mihály Makkai, (Eds. B. Hart et al), CRM Proceedings and Lecture Notes
American Mathematical Society, 53:177–188, 2011

- 18. Generalised Hasse-Schmidt varieties and their jet spaces (with T. Scanlon) Proceedings of the London Math. Society, 103(2):197–234, 2011
- 17. Model theory and complex geometry (Feature article, invited submission) Notices of the American Mathematical Society, 57(2):230–235, 2010
- 16. Jet and prolongation spaces (with T. Scanlon) Journal de l'Institut de Mathématiques de Jussieu, 9(2):391–431, 2010
- 15. On canonical bases and internality criteria (with A. Pillay) Illinois Journal of Mathematics, 52(3):901–917, 2008
- 14. An essentially saturated surface not of Kähler-type (with R. Moraru and M. Toma)
  Bulletin of the London Mathematical Society, 40(5):845–854, 2008
- 13. Differential arcs and regular types in differential fields (with A. Pillay and T. Scanlon)

  Journal für die reine und angewandte Mathematik, 620:35–54, 2008
- 12.K-analytic vs CCM-analytic sets in nonstandard compact complex manifolds (with S. Starchenko), Fundamenta Mathematicae, 198(2):139–148, 2008
- 11. Model Theory and Kähler Geometry (with A. Pillay)

  Model Theory with Applications to Algebra and Analysis Vol. 1

  (Eds. Z. Chatzidakis et al), Cambridge University Press, 167–195, 2008
- 10. Stable definability and generic relations (with B. Kim) Journal of Symbolic Logic, 72(4):1163–1176, 2007
- 9. Division points on subvarieties of isotrivial semiabelian varieties (with D. Ghioca) International Mathematics Research Notices, Article ID 65437, 23 pages, 2006
- 8. Strongly minimal groups in the theory of compact complex spaces (with M. Aschenbrenner and T. Scanlon)
  Journal of Symbolic Logic, 71(2):529–552, 2006
- 7. On saturation and the model theory of compact Kähler manifolds Journal für die reine und angewandte Mathematik, 586:1–20, 2005
- 6. The model theory of compact complex spaces. Logic Colloquium '01 (Eds. M. Baaz et al), Association for Symbolic Logic, 317–349, 2005

- 5. A nonstandard Riemann existence theorem Transactions of the American Mathematical Society, 356(5):1781–1797, 2004
- 4. F-structures and integral points on semi-abelian varieties over finite fields (with T. Scanlon)

American Journal of Mathematics, 126(3):473–522, 2004

- 3. The Mordell-Lang conjecture in positive characteristic revisited (with T. Scanlon), Model Theory and Applications (Eds. L. Bélair et al), Seconda Università di Napoli, 275–296, 2002
- 2. On difference fields with quantifier elimination Bulletin of the London Mathematical Society, 33(6):641–646, 2001
- 1. A note on uniform definability and minimal fields of definition Journal of Symbolic Logic, 65(2):817–821, 2000

# Invited Participation at Institute Workshops

#### Fields Institute Toronto

Trends in Pure and Applied Model Theory

July 1 – December 31, 2021

# Institut Henry Poincaré Paris, France

Model Theory and Applications

March 26–30, 2018

#### Luminy CIRM, France

Alg., Arith. and Comb. of Difference/Differential Equations May 28–June 1, 2018 Model Theory, Difference/Differential Equations and Applications April 7–10, 2015 The Geometry of the Frobenius Automorphism March 25–29, 2013 MODNET workshop on Model Theory of Fields November 12–16, 2007

#### **Oberwolfach** Mathematisches Forschungsinstitut, Germany

Model Theory: groups, geometries and combinatorics	January 2020
Model Theory: groups, geometry, and combinatorics	January 3–9, 2016
Around Valued Fields and Dependent Theories	January 3–9, 2010
Model Theory and Groups	Janunary 14–20, 2007
Model Theory and Complex Analytic Geometry	July 18–24, 2004

# Durham Symposium London Math. Society, United Kingdom

New Directions in the Model Theory of Fields

July 20–30, 2009

#### **BIRS** Alberta

Alg. Dynamics and Difference/Differential Eqns	Scheduled for Nov 2020
Stability Theoretic Methods in Unstable Theories	February 8–13, 2009
Interactions between Model Theory and Geometry	March 13–18, 2004

# Invited Talks of the last five years

# Ranked groups: The return

Université Claude Bernard Lyon 1, France September 2021

"From Borovik-Cherlin to bounding nonminimality"

# North American Meeting of the ASL

Notre Dame University

June 2021

"Some model theory of automatic sets, I and II"

# Practical and Structural Model Theory

July 2020, cancelled

Passau, Germany

Model Theory Conference Karkonosze, Poland

June 2020, cancelled

# Interactions between Representation Theory and Model Theory

University of Kent, United Kingdom
"Model theory and the DME"

July 2019

# Manchester Logic Seminar

July 2019

"Pullbacks under the log derivative"

# Connections between Model Theory, Differential and Difference algebra, and their Applications, CUNY, New York "Pullbacks under the log derivative" March 2019

**Pure and Applied Model Theory**, University of Illinois at Chicago *October 2018* "Around Jouanolou-type Theorems"

#### Lyon Logic Seminar

June 2018

"The groupoid-cover correspondence revisited"

# Groupe d'Etude sur les Problèmes Diophantiens Paris

June 2018

"Isotrivial Mordell-Lang and finite automata"

# Algebra, Arith. and Combinatorics of Difference/Differential Equations CIRM, Luminy, France May 2018

"Around Jouanolou-type Theorems"

#### Géometrie et Théorie des Modèles Paris

May 2018

"Isotrivial Mordell-Lang and finite automata"

# Model Theory and Applications Institut Henri Poincaré, Paris March 2018 "D-varieties and the Dixmier-Moeglin equivalence"

#### Oxford Logic Seminar

February 2018

"Isotrivial Mordell-Lang and finite automata"

Bridges between Automatic Sequences and Algebra and CRM, Montreal, "F-sets, Mordell-Lang, and automaticity"	Number Theory May 2017
<b>Joint Math. Meetings</b> ASL Invited Address Atlanta, GA "An application of model theory to noncommutative algebra"	January 2017
Winter Meeting of the CMS Niagara Falls, Ontario Special Session on Mathematical Logic "An application of model theory to noncommutative algebra"	December 2016
Thematic Program in Model Theory Notre Dame "An application of model theory to Hopf Ore extensions"	June 2016
Differential Algebra Mini-Workshop CUNY, New York	May 2016

# Supervisory Experience

"The differential Dixmier-Moeglin problem"

Post-doctoral	
Léo Jiminez	2021-
Dino Rossegger (co-supervisor)	2019 – 2021
Simon Crawford (co-supervisor)	2018-2020
Rémi Jaoui	2017-2019
Levon Haykazyan	2016 – 2019
Yi Zhu (co-supervisor)	2015-2017
Jonathon Stephenson (co-supervisor)	2015-2017
Alex Wires (co-supervisor)	2013-2015
Pantelis Eleftheriou	2011-2013
Javier Moreno	2011
Bernie Anderson (co-supervisor)	2009-2011
Moshe Kamensky	2007-2009

#### **Doctoral**

Christine Eagles 2021– Christopher Hawthorne 2017–2021 Ruizhang Jin  $^1$  2013–2019

Thesis: The Log Derivative and Model-Theoretic Analysability in DCF

Omar León Sánchez<sup>2</sup> 2008-2013

Thesis: Contributions to the model theory of partial differential fields

<sup>&</sup>lt;sup>1</sup>Winner of the faculty wide 2019 Huawei Prize for Best Research Paper

<sup>&</sup>lt;sup>2</sup>Winner of the faculty-wide 2013 Murray Martin Prize for graduate research

#### Masters

Christine Eagles	2020 – 2021
Marco Handa	2019-2020
Wilson Poulter	2018-2019
Essay: Zilber's principle in practice	
Hussein Ahmed (co-supervisor)	2017-2018
Essay: Gödel's 2nd incompleteness theorem and fragments of arithme	etic
Christopher Hawthorne	2015-2016
Essay: Formal languages and the model theory of finitely generated for	ree monoids
Ruizhang Jin	2012-2013
Essay: Canonical bases in stable theories	
Daniel Ivan	2011 - 2012
Essay: Existentially closed Hasse fields	
Allen O'Hara	2010 – 2011
Essay: An introduction to equations and equational theories	
Chris Eagle	2008-2010
Thesis: The Mordell-Lang theorem from the Zilber dichotomy	

# Undergraduate, NSERC

Austin Shiner (Spring 2020), Alexander Slamen (Spring 2020), Spencer Wilson (Fall 2019), Garret Hildebrandt (Spring 2019), Nicole Chassin (Spring 2016, Fall 2015), Michael Zhu (Winter 2016), Christopher Hawthorne (Spring 2013), Eeshan Wagh (Spring 2013), Yossef Musleh (Winter 2013), Chen Fei Du (Fall 2011), Matthew Harrison-Trainor<sup>3</sup> (Spring 2010, Spring 2011), Jack Klys (Spring 2010), Oleg Chterental (Winter 2009), Richard Zsolt (Spring 2008), Elliot Lipnowski (Winter 2008), Wilson Kan (Spring 2006)

### Undergraduate, Other

Shuo (Spencer) Gao (Spring 2020), Lirong Yang (Winter 2017, Winter 2015), Alan Yeung (CUHK, Spring 2016), Li Yan Lung (CUHK, Spring 2015) Atul Sivaswamy (Spring 2009).

#### **Doctoral Thesis Committees**

Léo Jiminez, Notre Dame University (external examiner)	2020
Hongdi Huang, University of Waterloo Pure Math	2020
Michael Deveau, University of Waterloo Pure Math	2019
Mohammad Mahmoud, University of Waterloo Pure Math	2019
Blake Madill, University of Waterloo Pure Math	2017
Ian Payne, University of Waterloo Pure Math	2017
Tyrone Ghaswala, University of Waterloo Pure Math	2017
Diana Castenada (oral comp examiner), University of Waterloo Pure Math	2017
Matthew Luther, McMaster University, Math & Statistics (external reader)	2015

<sup>&</sup>lt;sup>3</sup>Winner of the faculty-wide 2012 Jesse W.H. Zou Memorial Award for undergraduate research

Robert Garbary, University of Waterloo Pure Math	2015
Carolyn Knoll, University of Waterloo Pure Math	2013
Rohan Kapadia, University of Waterloo C&O (internal-external reader)	2013
James Frietag, University of Illinois at Chicago (external reader)	2012
Jean-Martin Albert, McMaster University (external reader)	2010
Dale Radin, University of Illinois at Chicago (external reader)	2004

# Masters Essay/Thesis Committees

Jake Zimmerman (2018), Chris Dugdale (2014), David Peterson (2013), Siwei Gao (2012), David Belanger (2009), Zi Yang Sham (2008), Stephanie Kleven (2006)

# **Teaching** at the University of Waterloo in the last five years

Topics in Logic: **Model theory of fields with operators** PMath 930 Winter 2021 (7 students), Fall 2019 (5 students)

# Linear Algebra 2, advanced Math 245

Fall 2020 (32 students), Fall 2019 (44 students)

# Set Theory and Model Theory PMath 733 (formerly 433/633)

Fall 2020 (37 students), Fall 2018 (28 students), Fall 2016 (24 students), Winter 2015 (21 students), Fall 2012 (22 students), Fall 2010 (28 students), Fall 2008 (37 students)

# Introduction to Commutative Algebra PMath 446/646

Winter 2020 (21 students), Winter 2019 (30 students), Winter 2016 (18 students)

# Algebra for Honours Mathematics Math 135

Winter 2019 (57 students), Fall 2017 (38 students), Winter 2017 (63 students), Fall 2016 (51 students), Fall 2013 (175 students), Fall 2012 (162 students), Fall 2011 (172 students), Winter 2011 (88 students), Fall 2009 (143 students), Fall 2004 (140 students)

# Groups and Rings PMath 347

Fall 2017 (52 students), Fall 2015 (36 students)

# Topics in Algebra: Valued Fields PMath 900

Winter 2017 (17 students), Fall 2013 (16 students), Fall 2011 (18 students)

# Service

Canadian Mathematical Society, Vice-President Ontario CMS Ambassador	2015–2017 2018–	
Waterloo Committees		
Departmental Colloquium Chair, Department Advisory Committee on Appointmental Tenure and Promotions, Graduate Studies, Undergraduat Scholarships, Library Representative	· -	
Faculty Working Group on Black and Indigenous Racism Faculty Working Group on Research, Creativity, and Innovation Research Advisory Committee; Nominating Committee for Chair University	•	
Faculty Association Departmental Representative; Academic Free Committee; Hagey Lecture Committee (Chair); CEMC Advisory Appointments; PhD Defense Chair pool		е
Conference Organising Committees		
Thematic Programme on Trends in Pure and Applied Model Theory		
	July-Dec 2021	
Workshop on Model Theory of Differential Equations, Algebraic Geom	-	
and their Applications to Modeling, BIRS	May 2020	
CMS Winter Meeting, Special Session on Model Theory	Ü	
<u> </u>	December 2019	
Workshop on Recent Applications of Model Theory	2010	
Fields Institute	July 2019	
Model Theory Special Session, ASL Annual Meeting	0 dig 2019	
City University of New York	May 2019	
v	May 2019	
CMS Winter Meeting, Special Session on Model Theory Waterloo  L	December 2017	
Workshop on Differential Galois Theory and Differential Algebraic Gro	-	
Fields Institute	July 2017	
Workshop on Model Theory and Arithmetic Dynamics	I 1 2012	
Fields Institute	July 2016	
- ' ' ' ' ' ' ' ' ' ' ' ' ' ' ' ' ' ' '	February 2014	
ASL Annual Meeting, Waterloo	May 2013	
Model Theory Special Session, ASL Annual Meeting, Waterloo	May 2013	
IMNA (Chair), Max Planck Institute for Mathematics, Bonn	June 2012	
Recent Developments in Model Theory, Oléron, France	June 2011	
ASL Annual Meeting, Notre Dame	May 2009	
Model theory session of the CMS-MITACS Joint Conference, Winnipe	g <i>June 2007</i>	

Greater Boston Logic Conference, MIT

May 2003