## Assignment 2

Translate each of the following four syllogisms into equational arguments.
(1) All M is P. $=0$

| All S is M. | $=0$ |
| :--- | :--- |
| All S is P. | $=0$ |

(2) All M is P. $\quad=0$

| No $S$ is $M$. | $=0$ |
| :--- | :--- |
| No $S$ is $P$. | $=0$ |

(3)

| All P is M. | $=0$ |
| :--- | :--- |
| No M is S. | $=0$ |
| No S is P. | $=0$ |


| (4) |
| :---: |
|  |
|  |

No M is P .
$=0$

| All $S$ is M. | $=0$ |
| :--- | :--- |
| No $S$ is $P$. | $=0$ |

(a)

(b)
(c)

(d)

(e)



Which of the six diagrams above could qualify as Venn diagrams?
Answer: $\qquad$

## The Expansion Theorem

For the formula $F(A, B)=(A B)^{\prime}$ carry out the following computations to calculate the expansion of $F(A, B)$ on $A, B$ :

$$
\text { Full Expression } \quad \text { Value }
$$

| $F(1,1)=$ | $=$ |
| :--- | :--- |
| $F(1,0)=$ | $=$ |
| $F(0,1)=$ | $=$ |
| $F(0,0)=$ | $=$ |

Thus expanding on $A, B$ gives: $F(A, B)=$
For the formula $F(A, B, C)=(A B)^{\prime} \cup(B C)$ carry out the following computations to calculate the expansion of $F(A, B, C)$ on $A$ :

|  | Full Expression | Simplified |
| :--- | :--- | :--- |
| $F(1, B, C)=$ |  |  |
| $F(0, B, C)=$ | $=$ |  |

Expanding on $A$ gives: $F(A, B, C)=$

For the formula $F(A, B, C)=(A B)^{\prime} \cup(B C)$ carry out the following computations to calculate the expansion of $F(A, B, C)$ on $B, C$ :

|  | Full Expression |  |
| :--- | :--- | :--- |
| $F(A, 1,1)=$ | Simplified |  |
| $F(A, 1,0)=$ | $=$ |  |
| $F(A, 0,1)=$ | $=$ |  |
| $F(A, 0,0)=$ | $=$ |  |

Expanding on $B, C$ gives: $F(A, B, C)=$ $\qquad$

## Elimination

For the formula $E(A, B, C)=\left(A\left(A^{\prime} \cup B\right)^{\prime} C^{\prime}\right)^{\prime}$ carry out the following computations to eliminate $A$ from the equation $E(A, B, C)=0$ :

|  | Full Expression |  |
| :--- | :--- | :--- |
| $E(1, B, C)=$ |  | Simplified |
| $E(0, B, C)=$ |  | $=$ |

Eliminating $A$ gives (simplify first!): $\quad=0$

For the formula $E(A, B, C, D)=(A \cup B)(C \cup D)$ carry out the following computations to eliminate $B, C$ from the equation $E(A, B, C, D)=0$ :

|  | Full Expression |  |
| :--- | :--- | :--- |
| $E(A, 1,1, D)=$ |  | Simplified |
| $E(A, 1,0, D)=$ | $=$ |  |
| $E(A, 0,1, D)=$ | $=$ |  |
| $E(A, 0,0, D)=$ | $=$ |  |

Eliminating $B, C$ gives (simplify first!):

$$
=0
$$

Fill in the following tree to give a proof of the validity of the argument using the method of Lewis Carroll. Be sure to give the number for each boxed letter.


