## Assignment 2

Translate each of the following four syllogisms into equational arguments.



Which of the six diagrams above could qualify as Venn diagrams?

Answer:

## The Expansion Theorem

For the formula F(A, B) = (AB)' carry out the following computations to calculate the expansion of F(A, B) on A, B:

/	,	Full Expression	Value
	F(1,1) =		=
	F(1,0) =		=
	F(0,1) =		=
	F(0,0) =		=

Thus expanding on A, B gives: F(A, B) =

For the formula  $F(A, B, C) = (AB)' \cup (BC)$  carry out the following computations to calculate the expansion of F(A, B, C) on A:

	Full Expression	Simplified
F(1, B, C) =		=
F(0, B, C) =		=

Expanding on A gives: F(A, B, C) =

For the formula  $F(A, B, C) = (AB)' \cup (BC)$  carry out the following computations to calculate the expansion of F(A, B, C) on B, C:

	Full Expression	Simplified
F(A, 1, 1) =	=	
F(A, 1, 0) =	=	
F(A,0,1) =	=	
F(A, 0, 0) =	=	

Expanding on B, C gives: F(A, B, C) =

## Elimination

For the formula  $E(A, B, C) = (A(A' \cup B)'C')'$  carry out the following computations to eliminate A from the equation E(A, B, C) = 0:

	Full Expression		Simplified
E(1, B, C) =		=	
E(0, B, C) =		=	

Eliminating A gives (simplify first!): = 0

For the formula  $E(A, B, C, D) = (A \cup B)(C \cup D)$  carry out the following computations to eliminate B, C from the equation E(A, B, C, D) = 0:

	Full Expression	Simplified
E(A, 1, 1, D) =	=	
E(A, 1, 0, D) =	=	
E(A, 0, 1, D) =	=	
E(A, 0, 0, D) =	=	
Eliminating $B, C$ gives (simplify first	!): = 0	

Fill in the following tree to give a proof of the validity of the argument using the method of Lewis Carroll. Be sure to give the number for each boxed letter.

1 ACL	= 0
2 A'I'M	´= 0
3 <i>GIO</i> ′	= 0
4 A'CM	= 0
5 <i>CIO</i>	´ = 0
LO'G	= 0

