Put the following formula in prenex form. Use capital letters when renaming variables. Show details of your work:

$$\forall u \left(u < y \right) \rightarrow \exists y \forall z \left[\neg \left(u + y < w + z \right) \rightarrow \neg \exists w \left(w \cdot y < w \cdot z \right) \right]$$

Answer:

DETAILS

Convert the following argument into a set \mathcal{C} of clauses such that the argument is valid iff the set \mathcal{C} is not satisfiable. Use capital letters when changing the names of variables. Show details of your work.

$$\forall x \Big(\exists y \, (x \cdot y < x) \ \to \exists z \, \big((y \cdot z < x) \land \neg (y \cdot x < z) \big) \Big) \quad \therefore \ \exists x \forall y \, (x \cdot y < y)$$

Answer:

DETAILS: