Name: ID:

PMath 330

Assignment 1

Mark______

Complete the following from Appendix B.

Lemma B.0.18 $(a \cdot b)^n = a^n \cdot b^n$.

PROOF. By induction on n.
For $n = 1$:

$$
\begin{aligned}
(a \cdot b)^1 &= a \cdot b && \text{by } \boxed{} \\
&= a^1 \cdot b^1. && \text{by } \boxed{}
\end{aligned}
$$

Induction Hypothesis: $(a \cdot b)^n = a^n \cdot b^n$.

$$
\begin{aligned}
\text{Thus } (a \cdot b)^{n'} &= (a \cdot b)^n \cdot (a \cdot b) && \text{by } \boxed{} \\
&= ((a \cdot b)^n \cdot a) \cdot b && \text{by } \boxed{} \\
&= (a \cdot (a \cdot b)^n) \cdot b && \text{by } \boxed{} \\
&= (a \cdot (a^n \cdot b^n)) \cdot b && \text{by } \boxed{} \\
&= ((a \cdot a^n) \cdot b^n) \cdot b && \text{by } \boxed{} \\
&= ((a^n \cdot a) \cdot b^n) \cdot b && \text{by } \boxed{} \\
&= (a^{n'} \cdot b^n) \cdot b && \text{by } \boxed{} \\
&= a^{n'} \cdot (b^n \cdot b) && \text{by } \boxed{} \\
&= a^{n'} \cdot b^{n'}. && \text{by } \boxed{}
\end{aligned}
$$

Six Syllogisms

(1) All P is M.
Some M is S.
____
Some S is P.

(2) All M is S.
Some P is M.
____
Some S is P.

(3) Some M is not S.
No M is P.
____
Some S is not P.

(4) Some P is M.
No S is M.
____
Some S is not P.

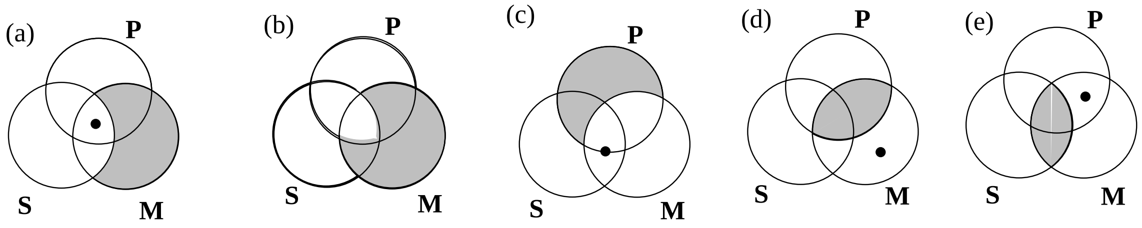
(5) Some S is M.
All P is M.
____
Some S is P.

(6) All M is P.
All M is S.
____
Some P is S.

For each of the above syllogisms find the **figure** and the **mood**, and determine if it is valid under Aristotle's Convention (AC), and if it is valid under the Modern Convention (MC).

	Figure	Mood	Valid under (AC)	Valid under (MC)
1				
2				
3				
4				
5				
6				

Five Venn Diagrams



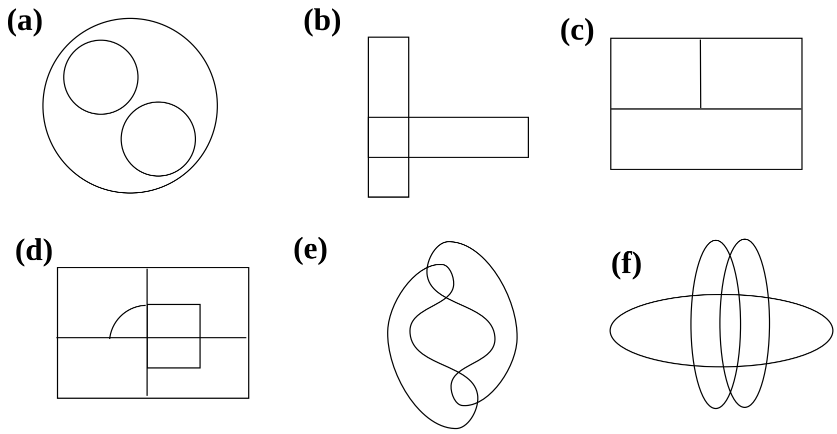
For each of the six syllogisms at the top find the Venn diagram for its premisses from the above and enter the answers in the empty boxes below:

Syllogism	1	2	3	4	5	6
Venn Diagram						

Translate each of the following four syllogisms into equational arguments.

(1)	No P is M.	$= 0$	(2)	No M is S.	$= 0$
	No M is S.	$= 0$		All M is P.	$= 0$
	All S is P.	$= 0$		No S is P.	$= 0$
(3)	No M is P.	$= 0$	(4)	All P is M.	$= 0$
	All S is M.	$= 0$		No M is P.	$= 0$
	No S is P.	$= 0$		All S is P.	$= 0$

Which of the six diagrams below could qualify as **Venn diagrams**?



Answer: ____________________