# COMBINATORICS OF FEYNMAN DIAGRAMS LECTURE 27 SUMMARY

#### WINTER 2018

## SUMMARY

With notation and assumptions from the end of last class, Foissy's theorem is

**Theorem 1.** The following are equivalent:

(1)  $T(x) = xB_+(f(T(x)) \text{ is Hopf}$ (2) f(z) is one of the following • f(z) = 1, or

• 
$$f(z) = e^{\alpha z}, \ \alpha \neq 0, \ or$$

• 
$$f(z) = (1 - \alpha\beta z)^{-\frac{1}{\beta}}, \ \alpha\beta \neq 0.$$

(3) There exists 
$$\alpha, \beta$$
 such that

$$(1 - \alpha\beta z)f'(z) = \alpha f(z)$$
$$f(0) = 1$$

We went over some of the key ideas in the proof. Some of the calculations are also in your assignment. Then we finished with the binary tree example up to order 4 just checking by hand that it really is Hopf.

#### NEXT TIME

Next class we'll think about more physical DSEs.

## References

Foissy's paper is arXiv:0707.1204